CS6375: Machine Learning Gautam Kunapuli

Final Exam Review



Final Exam

Topics:

- Ensemble methods
 - Bagging
 - Boosting
- Clustering
 - K-Means
 - Hierarchical clustering
 - Soft clustering & Gaussian Mixture Models
- **Dimensionality Reduction**: Principal Component Analysis
- Neural Networks
- Reinforcement Learning

Ensemble Methods

- Error = Variance + Bias² + Noise²
 - Intuition: When combining multiple independent decisions, random errors cancel each other out
- Two main methods Bagging and Boosting
- **Bagging**: Combines several learned models that are learned *independently* from **bootstrap replicates** of the same data set.
 - What does bagging remove? Bias or variance?
 - Reduce variance without increasing bias by averaging
 - What are the best ones to bag? Trees? Linear regression? Nearest neighbors?
- Boosting: Learns a weighted combination of classifiers. Focuses on the incorrectly classified part of the data set
 - What does boosting address? Bias or variance?
 - Reduce bias and variance
 - What is AdaBoost?
 - How does AdaBoost weight examples?
 - What are good weak learners?
 - How does boosting avoid overfitting?
 - Margins!
 - Remember, boosting is <u>not</u> immune to overfitting
- How do ensemble methods work with stable algorithms? Outliers?

Clustering: K-Means

- Euclidean distance is used as a metric and variance is used as a measure of cluster scatter
 - What are other distance measures?
- *k* is an input parameter: inappropriate choice of *k* may yield poor results.
- Convergence to local minimum
 - may produce counterintuitive results
- What are responsibilities? What is the loss function of k-means clustering?
- What is the computational complexity of k-means?
- What type of clusters does k-means generate?

k-means Clustering

Given: Unlabeled data, x_i , i = 1, ..., n**Initialize**: Pick k random points as cluster centers μ_j , j = 1, ..., k

while not converged do

- Assign data points x_i to closest cluster center μ_j
- **Update** the cluster centers μ_j to the mean (average) of the points assigned to that cluster
- if the assignments no longer change, **converged** = **true**





(a)

(d)

Hierarchical Clustering

Bottom-up (agglomerative): Recursively merge two groups with the smallest between-cluster similarity
Top-down (divisive): Recursively split a leastcoherent (e.g. largest diameter) cluster



Differences between different types of linkages:

Closest pair (single-link clustering) tends to yield elongated clusters

Farthest pair (complete-link clustering) tends to yield rounder, more spherical clusters

Average of all pairs trades-off between single and complete link

Closest pair (single-link clustering)



Farthest pair (complete-link clustering)



Gaussian Mixture Models

Probabilistic clustering (generative model):

Each cluster is associated with a Gaussian distribution. To generate data,

- randomly choose a cluster *j* with probability P(y = j)
 - distribution over the clusters is modeled as a multinomial distribution
- generate from the distribution of the *j*-th cluster:
 - distribution over each cluster is modeled as a multivariate Gaussian distribution



Solved using Expectation Maximization

- soft assignment of points to clusters
- maximize log likelihood.
- Can be used for non-spherical clusters with different probabilities





Principal Component Analysis

- Can be used to **reduce the dimensionality** of the data **while still maintaining a good approximation** of the sample mean and variance
- Can also be used for **selecting good features** that are combinations of the input features
- **Unsupervised** just finds a good representation of the data in terms of combinations of the input features

Principal Component Analysis identifies the principal compone in the **sample covariance matrix** of the data, $X^T X$ (*note that since our data is #examples (n) x features (d), the covariance matrix will be d × d*)

- PCA finds a set of **orthogonal vectors** that **best explain the variance of the sample covariance matrix**
- These are exactly the **eigenvectors** of the covariance matrix $X^T X$
- We can **discard the eigenvectors** corresponding to small magnitude eigenvalues to yield an approximation
- **Simple algorithm** to describe, MATLAB and other programming languages have built in **support** for eigenvector/eigenvalue computations



- How to geometrically identify principal components, projections and effectiveness for classification?
- How do we select an ideal number of principal components?
- What are the properties of eigenvalues and eigenvectors?

Neural Networks

- Universal approximators
 - Representing Boolean functions and logical formulas
 - Representing general mathematical functions
- Various propagation aspects of neural networks
 - functional representation of outputs and inputs
 - gradient expressions
 - activation functions and properties (sigmoid, tanh, ReIU)
- Trained using backpropagation
 - forward propagation
 - backward propagation
- Overfitting in neural networks
 - regularization, dropout, other strategies
 - bias-variance tradeoff





Reinforcement Learning

Modeling RL as a Markov Decision Process

• set of states S, set of actions A, initial state S_0

for grid world, can be cell coordinates
transition model P(s, a, s')

•
$$P([1,1], \uparrow, [1,2]) = 0.8$$

• reward function r(s)

$$r([3,4]) = +1$$

discount factor

• learn a policy: mapping from *S* to *A*

• $\pi(s)$ or $\pi(s, a)$ (deterministic vs. stochastic)

Value functions

• Which states and actions are better?

Bellman equations, Bellman optimality conditions

- What is the difference between value iteration and policy iteration?
 - What is the value iteration update equation?
- What is the exploration vs. exploitation tradeoff?
- What is the **Q-learning**?
 - Why is Q-learning called model-free learning?



